DEPENDENCE OF Z-SCAN MEASUREMENTS ON THE SPATIOTEMPORAL PULSE PARAMETERS

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We report the experimental results obtained by the closed-aperture Z-scan technique where Nd:YAG minilaser short pulses with different temporal pulse shapes have been used. It is shown that the nonlinear refractive index coefficient n_2 of fused silica (one of the smallest among the condensed media) can be successfully measured using the pulses with durations of about 1 ns and energies less than 1 mJ. Very good compatibility between the values for the same samples of fused silica is obtained only if the temporal shapes of the used SBS-compressed, single longitudinal or multi longitudinal mode pulses are properly taken into account. It is also shown that spatial properties of the used beams should be taken account of properly. By these experiments we emphasize the significance of taking into account the temporal pulse shape profile for accurate determination of the nonlinear refractive index by the Z-scan technique.

Keywords: Z-scan, pulse shape, nonlinear refractive index, fused silica

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1. Introduction

The characterization of nonlinear optical properties of materials is of considerable interest, both from the fundamental and applied points of view. In particular, great effort has been devoted to the determination of nonlinear refraction (NLR) and absorption (NLA) mechanisms and magnitudes of different materials [1-4]. There are a number of methods for nonlinear refraction index n_2 measurements, but the most popular of them is the Z-scan method [1-11], introduced about twenty years ago (the history of Z-scan "discovering" see in [6]). A keen interest has lately been shown to the accuracy and reliability of the results obtained by means of this method, the main attention being paid to the influence of the finite aperture size, the thickness of samples, beam quality ratio, and similar problems [1–14]. Although hundreds of papers on Z-scan measurements were published and lasers with different pulse shapes and durations were used, only the original paper [5], the review papers [1-4, 7, 8], and a few others [14, 15] obviously indicate that the results must be temporally averaged properly when the non-rectangular pulses are used. The detailed analysis of the Z-scan theoretical background with emphasis on the temporal pulse shape dependence was presented in [16]. It gives a useful insight into important aspects of the Z-scan technique that are usually overlooked. In this paper we present the experimental results of the Z-scan measurements obtained using pulses with different pulse shapes for fused silica for which magnitudes of the nonlinear coefficient n_2 are well established using different measurement methods [3, 17–22]. The obtained results show that measured Z-scan data should be properly processed for extracting the correct values of the optical Kerr nonlinear coefficient.

2. Experimental set-up for the Z-scan measurements

For the measurements of n_2 in fused silica with different pulse shapes we used a standard closedaperture Z-scan experimental scheme for isotropic media (Fig. 1). Linearly polarized pulses were focused by lens L1 onto a sample which was moved along the z axis by the translation stage. The $\lambda/2$ phase plate and dielectric polarizer P were used to change the energy of the incident pulses. Laser pulses after the lens L1 were divided by a beam splitter BS. Reflected part of pulses was directed to the reference photodiode PD1. An aperture transmitting about 10% of the laser pulse energy (without the sample) was placed in the far field



Fig. 1. Experimental set-up: Nd:YAG minilaser with or without SBS-compressor, focusing lenses *L1* and *L2*, beam splitter *BS*, photodiodes *PD1* and *PD2*, diaphragm *D*.

of the beam transmitted by the sample. The energy of pulses transmitted through the aperture was measured with the photodiode PD2 placed directly after the aper-Both photodiodes were synchronized with the ture. laser. The translation stage and photodiodes through the controller were connected with a personal computer. Therefore, getting and processing of the experimental data were fully computer-assisted. At each zposition fifty measurements were done. For every laser pulse the data got from the photodiode PD2 were divided by data got from the photodiode PD1. Then the average value and dispersion of these ratios were accepted for further processing. We used fused silica KU-1 plates with thickness of about 6 mm as samples for the measurements.

It is well known that the nonlinear coefficient of the optical Kerr effect in fused silica is rather low [17–22]. So, a high intensity of laser pulses is needed for Z-scan measurements. Therefore, we have tried first to use short pulses obtained from a SBS-compressor with tetrachloride liquid cell [23]. The SBS-compressor was pumped by a flash lamp pumped Nd:YAG master oscillator with an active electrooptical Q-switch Pockels cell with negative feedback. It generated single longitudinal mode (SLM) pulses with energy of about 4 mJ and of 2-4 ns adjustable duration at a repetition rate of 5 Hz. Duration of the pulses and their shapes were measured with a system consisting of a fast photoelectric cathode connected to the analogue C7-19 oscilloscope having 5 GHz bandwidth. A typical digitized pulse shape of compressed pulses with measured duration $au_{
m m}$ is presented in Fig. 2(a). Taking into account the long enough rise time $\tau_{\rm d} \approx 100$ ps of the detection system, the real pulse width of compressed pulses can be evaluated as $\tau_r=(\tau_m^2-\tau_d)^{1/2}\approx$ 190 ps (FWHM). The energy of compressed pulses was about 2 mJ and could be amplified up to 16 mJ by the two-pass Nd:YAG amplifier. The amplified pulses were spatially filtered and after the beam cleanup procedure their beam transverse spatial profile was close to Gaussian. During

the Z-scan experiments the energy of pulses was controlled by the attenuator consisting of $\lambda/2$ plate and a dielectric polarizer. The experiments carried out with the SBS pulse compression system have shown that for the measurements of the nonlinear coefficient n_2 of fused silica using the Z-scan technique it is enough to have pulses with energies in the interval of 0.85–1.3 mJ when the focusing lens L1 with f = 30 cm is applied.

The diode pumped actively Q-switched Nd:YAG minilaser ($\lambda_{\rm p} = 1064$ nm, pulse repetition rate $\nu_{\rm p} =$ 25 Hz) was used in the other set of experiments. The main advantage of this laser is its ability to generate not only SLM pulses (Fig. 2(b)) of about $\tau_{\rm p} = 1.36$ ns (FWHM) duration, but also multi longitudinal mode (MLM) pulses (Fig. 2(c)). The maximum pulse energy $W_{\rm p}$ was about 1.7 mJ when the SLM pulses were generated. The transverse laser mode was also close to the TEM_{00} mode (controlled with CCD camera) and neither the laser transverse mode nor the beam waist radius w_0 did change practically while switching between SLM or MLM pulse generation regimes. The pulse shapes were in-situ sampled using a fibre-coupled fast InGaAs photodetector (DET01CFC/M, Thorlabs, rise time $\tau_{\rm d} = 100$ ps) connected to the fast digital oscilloscope having a 12 GHz bandwidth (TDS6124C, *Tektronix*). We will not describe our laser in detail here, but just indicate that switching from the SLM to MLM pulse generation regime and vice versa is performed by turning off or on the prelasing regime of the laser. When prelasing regime is turned on and adjusted correctly, 99% of the generated pulses are SLM. When it is turned off, the MLM pulses having slightly higher energy are generated. Thus, this laser allowed us to carry out Z-scan experiments using SLM and MLM shaped pulses in the same focusing geometry and see what the difference in the measured Z-scan signal was and how to correctly extract the values of the n_2 coefficient from measured data.



Fig. 2. Shapes of pulses used in Z-scan experiments: (a) pulse shape of SBS-compressor, (b) SLM pulse shape, (c) typical MLM pulse shape. The durations $\tau_{\rm m}$ measured by oscilloscope are shown at the arrows.

3. Results and discussion

Before discussing the obtained results it is necessary to clarify the definitions and notations used. Selfaction effects studied in nonlinear optics have a long history [1–3, 24–27]. Therefore, the same notation n_2 for the nonlinear index coefficient (NIC) is often used, applying different definitions. Throughout this paper, we will employ n_2 for linear polarization defined via

$$\delta n(\boldsymbol{r},t) = n_2 \left\langle \tilde{\boldsymbol{E}}^2(\boldsymbol{r},t) \right\rangle, \qquad (1)$$

where the change of the refractive index $\delta n(\mathbf{r})$ locally depends on the time-averaged square of the electric field $\langle \tilde{\mathbf{E}}^2(\mathbf{r},t) \rangle$ in the medium. Taking into account that the optical intensity in the medium is defined as $I = c n_0 \langle \tilde{\mathbf{E}}^2(\mathbf{r},t) \rangle / (4\pi)$, ignoring nonlinear corrections for $n(\mathbf{r}) = n_0 + \delta n(\mathbf{r})$, the change of the refraction index n due to the optical Kerr effect can be expressed in terms of nonlinear indices n_2 (in esu units) or γ_2 (in SI units) through the relations

$$n(\mathbf{r},t) = n_0 + \frac{n}{2} |\mathbf{E}(\mathbf{r},t)|^2 = n_0 + \gamma_2 I(\mathbf{r},t),$$
 (2)

where n_0 is the linear part of the refractive index, E is the complex amplitude of the electric field of the beam,

$$\tilde{\boldsymbol{E}}(\boldsymbol{r},t) = \operatorname{Re}\boldsymbol{E}(\boldsymbol{r},t) \, \exp[\mathrm{i}(k_0 z - \omega t)], \quad (3)$$

and I denotes the intensity of the laser beam within the sample. $k_0 = n_0 \omega/c$ is the modulus of the wave vector, ω is the circular frequency. Coefficients n_2 and γ_2 are related through the conversion formula n_2 [esu] = $[c n_0/(40\pi)]\gamma_2$ [m² W⁻¹], where c is the speed of light in vacuum.

The study of the pulse shape influence is very important because in general the nonlinear refractive index is determined by several physical mechanisms, acting in a broad range of time scales [1-3, 24-27]. In non-resonant interactions and for pulse durations of about 1 ns the main mechanisms that contribute to the nonlinear index of refraction in solid state materials (for example, in fused silica) are electronic polarization and lattice vibrations. These mechanisms are very fast, with typical time responses of about $\sim 10^{-15}$ and $\sim 10^{-13}$ s, respectively [1–3]. Therefore, for pulse durations longer than 1-10 ps the cw case is valid. Vibrational (nuclear) contribution to the nonlinear index coefficient n_2 is significant enough (10–20% in glasses) [3]. The contribution of the electrostrictive effect is also often considered [1, 3]. According to [1], the electrostrictive NIC is $n_2^{\text{ES}} \sim 10^{-19} \text{ m}^2 \text{ V}^{-2}$, which is higher than optical Kerr NIC ($n_2^{\text{K}} \sim 10^{-22}$ – 10^{-21} m² V⁻²) for typical transparent dielectrics. But as shown by one of us previously [29], the contribution of the optical Kerr nonlinearity to the nonlinear change of the refractive index ($\Delta n_{\parallel}^{\rm K}(\omega) = 11.5 \cdot 10^{-14} E_0^2)$ induced by the Gaussian beam with linear polarization is by an order of magnitude stronger than the electrostrictive contribution $(\Delta n_{\parallel}^{\rm ES}(\omega) = 15.8 \cdot 10^{-15} E_0^2)$ at the axis of the beam for fused silica (here E_0 is the peak

strength of the electric field in esu units). It should also be noted that contrary to the common claims of the known textbooks and review articles [1, 3, 28], the electrostrictive change of the refractive index strongly depends on the polarization and the intensity distribution of the beam [29, 30]. Our evaluation of electrostrictive n_2^{ES} is consistent with a very rough estimate of the magnitude of the electrostrictive nonlinear index given in the new review [3]. It follows from [3] that the electrostrictive γ_2^{ES} is proportional to p_{11}^2 (p_{ij} are the elastoptical coefficients in Voigt notation) and its value is $0.4 \cdot 10^{-20} \text{ m}^2 \text{ W}^{-1}$. It can be shown that in another limiting case it is proportional to p_{12}^2 [30]. These Voigt coefficients differ strongly enough for fused silica: $p_{11} =$ 0.12 and $p_{12} = 0.27$ [30]. Thus, the electrostrictive contribution to NIC has typically amounted to tens of percent contribution to the Kerr effect in the stationary case [3]. Besides, it is very important that the electrostrictive response time, which is roughly equal to the time required for an acoustic deformation to travel across the diameter of the optical beam in the medium, is of about ~ 10 ns under our experimental conditions. Thus, the electrostrictive response is very slow, and therefore its contribution is very low as compared to the electronic and nuclear Kerr effect and cannot strongly influence our measurement results with short pulses. Time scales of thermal and other physical mechanisms of nonlinearities are even longer and do not contribute to the nonlinear transmittance in our measurements at low pulse repetition rates.

The detailed theoretical description of the procedure of taking into account the pulse shape temporal profile was done previously [16]. In the case of a small nonlinear phase change $|\Delta \Psi_0(t)| \ll 1$ at the beam waist position of the sample z_0 the theoretical normalized closed aperture Z-scan energy transmittance can be written as

$$T_{\rm th}(z, \langle \Delta \Psi_0(t) \rangle) \cong$$

$$1 + \frac{4\langle \Delta \Psi_0(t) \rangle (z - z_0) / z_{\rm R}}{\left[9 + (z - z_0)^2 / z_{\rm R}^2\right] \left[1 + (z - z_0)^2 / z_{\rm R}^2\right]}, \quad (4)$$

where

$$\left\langle \Delta \Psi_0(t) \right\rangle = \frac{\int\limits_{-\infty}^{\infty} \Delta \Psi_0(t) P(t) \, \mathrm{d}t}{\int\limits_{-\infty}^{\infty} P(t) \, \mathrm{d}t} \,, \tag{5}$$

is power P(t) weighted time-averaged on-axial nonlinear phase change at the beam waist.

When the pulse shape $|f_j(t)|^2$, the pulse energy W_L , and the intensity at the beam waist I_{0j} can be measured (here and afterwards index j denotes the particular pulse shape used in the experiment), then the nonlinear refractive index can be found using formula

$$\gamma_2 = \eta_j^{(1)} \, \frac{\langle \Delta \Psi_{0j}(t) \rangle_{\text{fit}}}{k \, L_{\text{eff}} \, I_{0j}} \,, \tag{6}$$

where $\Delta \Psi_{0j}(t) = k L_{\text{eff}} \gamma_2 I_{0j} |f_j(t)|^2$, $k = \omega/c = 2\pi/\lambda$ is the wave number for the wavelength λ in vacuum, $L_{\text{eff}} = (1 - e^{-\alpha L})/\alpha$, L is the thickness of the sample, α is the linear absorption coefficient. The coefficient $\eta_j^{(1)}$ describes the influence of the pulse shape and can be calculated by the formula [16]

$$\eta_{j}^{(1)} = \frac{\int_{-\infty}^{\infty} |f_{j}(t')|^{2} \mathrm{d}t'}{\int_{-\infty}^{\infty} |f_{j}(t')|^{4} \mathrm{d}t'},$$
(7)

where $|f_j(t')|^2$ is the experimentally sampled pulse shape, normalized to unity at the peak. While calculating the coefficient $\eta_j^{(1)}$, it is commonly assumed that the shapes of the pulse intensity and the pulse power are identical.

It is seen from the formula (6) that for the calculation of the nonlinear refractive index γ_2 the on axis beam intensity I_{0j} should be calculated. For Gaussian and near Gaussian beams with a known pulse shape this can be done using the formula

$$W_{\rm L} = \frac{\pi \, w_{0j}^2}{2} \, I_{0j} \, \tau_0 \int_{-\infty}^{\infty} |f_j(t')|^2 \mathrm{d}t' \,, \tag{8}$$

where the beam waist radius w_{0i} is defined using the second order moment method [31–33] and τ_0 is the time normalization unit. But simply measuring the beam waist radius w_{0j} is not enough because the transmittance described by the formula (4) depends on the Rayleigh length $z_{\rm R}$. Therefore, independent measurement of $z_{\rm R}$ should be carried out using the method of the second order moments [31-33]. As was shown in our papers [32, 33], the direct use of the alternative propagation ratios measured by varying the aperture, moving the knife or slit, which are not propagation invariants, is not appropriate for these purposes. But it can be shown that using special processing of the measured data obtained by the moving knife method the true invariant beam propagation ratio M^2 can be established not only for stigmatic beams [32, 33], but for general astigmatic beams as well. This specially developed procedure of measured data processing was used for measuring beam propagation ratios of SBS compressed pulses (Fig. 3(a)) and Nd: YAG minilaser pulses



Fig. 3. Beam radii measured by the moving knife method: (a) of the Nd:YAG laser with SBS-compressor, (b) of the diode pumped actively Q-switched Nd:YAG minilaser.

(Fig. 3(b)). This procedure allows getting values of the beam radii and appropriate beam propagation ratios pointed out in Fig. 3.

As follows from the formula (6), the main parameter needed for the determination of γ_2 value is the power-weighted time-averaged on-axial nonlinear phase change at the beam waist $\langle \Delta \Psi_0(t) \rangle$, which in the Z-scan method is found by fitting the measured transmittance data to the formula (4) of normalized transmittance. The fitting procedure is not commonly described in detail in the papers devoted to the measurement of NIC of materials by the Z-scan technique. But as will be shown in this paper the obtained values significantly depend on the used fitting procedure. It should be noted that the formula (4) is true only for the ideal case, when the transmittance normalization is performed very exactly and the scanning is done very perfectly. But it is very difficult experimentally to avoid the walk-off effect during scanning of the sample along the beam propagation direction. Therefore, we used the following formula for fitting of experimental data:

$$T_{\exp}(z, \langle \Delta \Psi_0(t) \rangle) \cong 1 + \frac{4 \langle \Delta \Psi_0(t) \rangle (z - z_0) / z_{\rm R}}{[9 + (z - z_0)^2 / z_{\rm R}^2] [1 + (z - z_0)^2 / z_{\rm R}^2]} + \Delta T - a(z - z_0), \qquad (9)$$

where the ΔT term corrects for the normalization error and the $a(z - z_0)$ term corrects for the walkoff effect.

First of all we present here the results of Z-scan measurements (Fig. 4(a)) using SBS-compressed pulses (Fig. 2(a)). For this pulse shape form calculated by formula (7) the value of the coefficient $\eta_{\text{SBS}}^{(1)}$ is 1.9. The energy $W_{\rm SBS}$ of used pulses was 0.85 mJ, $w_{0 \text{SBS}} = 84.5 \ \mu\text{m}$, and the correspondent intensity $I_{0 \text{ SBS}}$ at the beam waist obtained using formula (8) was 22.8 GW cm⁻². Finally, to find $\langle \Delta \Psi_0(t) \rangle$ and then γ_2 , using formula (6), we should use proper fitting of experimental data to formula (9). It should be noted that we can carry out this fitting procedure in different ways. Firstly, we can use the value of $z_{\rm R}$ found by independent measurement of $M^2 = 1.21$ (Fig. 3(a)). Another possibility is to assume that the used beam has practically a Gaussian transverse profile of intensity, and therefore we can fix $M^2 = 1.00$ and use an appropriate value of $z_{\rm R}$. And the third possibility is to alternate all parameters during the fitting procedure, including the values of $z_{\rm R}$. How the values of appropriate parameters are changing by using different fitting procedures (Fig. 4(a)) can be seen from Table 1.

 Table 1. Values of appropriate parameters obtained by different fitting procedures in the case when SBS-compressed pulses were used.

	$M^2 = 1.21$	$M^{2} = 1$	All parameters fitted
z_0	59.52±1.34 mm	59.32±1.78 mm	60.17±0.75 mm
$z_{ m R}$	17.41 mm (fixed)	21.07 mm (fixed)	11.90±1.12 mm
a	$(4.01\pm1.89)\cdot10^{-5}$	$(7.47 \pm 2.43) \cdot 10^{-5}$	$(-1.34 \pm 1.77) \cdot 10^{-5}$
ΔT	$(2.6\pm0.77)\cdot10^{-3}$	$(2.7\pm0.92)\cdot10^{-3}$	$(2.1\pm0.62)\cdot10^{-3}$
$\langle \Delta \Psi_0(t) \rangle$	$(1.11 \pm 0.08) \cdot 10^{-1}$	$(1.06 \pm 0.09) \cdot 10^{-1}$	$(1.33 \pm 0.11) \cdot 10^{-1}$
γ_2	$2.78 \cdot 10^{-16} \text{ cm}^2 \text{ W}^{-1}$	$2.65 \cdot 10^{-16} \text{ cm}^2 \text{ W}^{-1}$	$3.33 \cdot 10^{-16} \text{ cm}^2 \text{ W}^{-1}$
n_2	$0.96 \cdot 10^{-13}$ esu	$0.92 \cdot 10^{-13}$ esu	$1.15 \cdot 10^{-13}$ esu



Fig. 4. Z-scan dependences of the normalized transmittance versus the sample position when different pulses were used: (a) SBScompressed pulses, (b) SLM pulses, (c) MLM pulses.

The same processing procedure applied to the data obtained using SLM pulses (Fig. 2(b)) of the Nd:YAG minilaser (Fig. 4(b)) with the pulse energy $W_{\rm L} = 0.80$ mJ gives the results presented in Table 2. It is seen from these tables that the values of γ_2 obtained using values for $z_{\rm R}$ of independent measurements notably differ from the values of γ_2 calculated using other fitting methods. Although all obtained values for γ_2 are consistent with values for fused silica known from literature [3, 17–22], we assume that the values of γ_2 obtained by taking into account independent measure-

ments of $z_{\rm R}$ are preferable due to their more logical determination. It is significant also to note that for calculation of on-axis intensity the measured pulse profile with $\tau_{\rm m} = 210$ ps pulse duration (Fig. 2(a)) was used. The real pulse duration (as discussed previously) is notably shorter, $\tau_{\rm r} = 190$ ps, and the real on-axis intensity is higher. Therefore, we assume that the value of γ_2 can be evaluated more exactly using approximate formula $\gamma_2^* \approx \gamma_2 \tau_{\rm r}/\tau_{\rm m} \approx 2.52 \cdot 10^{-16} \ {\rm cm}^2 \ {\rm W}^{-1}$. Thus, the agreement between two independent measurements using different lasers is very good. It should also be

 Table 2. Values of appropriate parameters obtained by different fitting procedures in the case when SLM pulses were used.

	$M^2 = 1.33$	$M^{2} = 1$	All parameters fitted
z_0	74.43±0.32 mm	74.54±0.38 mm	74.50±0.34 mm
$z_{ m R}$	8.89 mm (fixed)	11.83 mm (fixed)	10.35±0.76 mm
a	$(-2.94\pm0.7)\cdot10^{-5}$	$(3.95 \pm 0.78) \cdot 10^{-5}$	$(-1.28\pm1.12)\cdot10^{-5}$
ΔT	$(3.50\pm0.17)\cdot10^{-3}$	$(3.50\pm0.17)\cdot10^{-3}$	$(3.50\pm0.17)\cdot10^{-3}$
$\langle \Delta \Psi_0(t) \rangle_{\rm fit}$	$(4.14 \pm 0.20) \cdot 10^{-2}$	$(3.98 \pm 0.19) \cdot 10^{-2}$	$(4.04 \pm 0.19) \cdot 10^{-2}$
γ_2	$2.55 \cdot 10^{-16} \text{ cm}^2 \text{ W}^{-1}$	$2.45 \cdot 10^{-16} \text{ cm}^2 \text{ W}^{-1}$	$2.49 \cdot 10^{-16} \text{ cm}^2 \text{ W}^{-1}$
n_2	$0.88 \cdot 10^{-13}$ esu	$0.85 \cdot 10^{-13}$ esu	$0.86 \cdot 10^{-13}$ esu

noted that the value of $z_{\rm R}$ obtained from the Z-scan data when all parameters of the transmittance formula (9) are fitted differs significantly from the directly measured one. Therefore, the method of $z_{\rm R}$ measurement by the Z-scan technique proposed in [34] can be used only if it is exactly known that the measured beam has exactly a Gaussian transverse structure.

We should note that it is very significant to take into account the real profile of used pulses. It can be illustrated by the case when SLM pulses are used in the Z-scan experiments. It can be seen from Fig. 2(b) that the temporal profiles of the generated pulses are very close to the Gaussian ones. Therefore, it seems that the use of corresponding values for $\eta_{\rm G}^{(1)} = \sqrt{2}$ and $I_{\rm G0} = 4\sqrt{\ln 2}W_{\rm L}/(\sqrt{\pi^3}\tau_{\rm G}w_{0\,\rm G}^2) = 8.78$ GW cm⁻² can be good enough. But the simple calculations used in obtaining results presented in Table 2 show that $\eta_{\rm SLM}^{(1)} = 1.56$ and $I_{0\,\rm SLM} = 7.53$ GW cm⁻². Thus, the approximation of the real SLM pulse profile by the Gaussian profile leads to the value of $\gamma_2 = 1.97 \cdot 10^{-16}$ cm² W⁻¹, i. e. 1.29 times lower than using the procedure discussed above.

The situation was more complicated when MLM pulses were used in the experiments. In this case due to interference of all existing modes in the resonator the temporal structure of the generated pulse shape is more complex (Fig. 2(c)). It should be noted that the shape of every generated pulse is always changed slightly, but the shown pulse shape is a typical one. The experiments show that the MLM pulses have practically the same energy $W_{\rm L}$ and spatial profile, i. e. the average waist radius ($\overline{w_0^2} \approx w_{0j}^2$) and the Rayleigh length $z_{\rm R}$ are practically equal to the same for SLM pulses. It is appropriate enough to assume that in this case the nonlinear refractive index can be found using properly averaged previously used formula (6):

$$\overline{\gamma_2} = \overline{\eta} \, \frac{\langle \Delta \Psi_{0j}(t) \rangle_{\text{fit}}}{k \, L_{\text{eff}} \, \overline{I_0}} \,, \tag{10}$$

2

where $\langle \Delta \Psi_{0j}(t) \rangle_{\rm fit}$ is again obtained from the fitting procedure for MLM pulses, $\bar{I}_0 = 2W_{\rm L}/(\pi \overline{w_0^2} \tau_0)$ is the reference intensity, and

$$\overline{\eta} = \frac{1}{N} \sum_{j=1}^{N} \frac{\left[\int_{-\infty}^{\infty} |f_j(t')|^2 \mathrm{d}t'\right]^2}{\int_{-\infty}^{\infty} |f_j(t')|^4 \mathrm{d}t'}, \qquad (11)$$

is a new averaged form-factor for MLM pulses. It is implicitly assumed that using every time large enough number of pulses for the averaging procedure this form-factor will be not changed. It seems that such data processing was used in [15], though it is not described in detail. Two types of the MLM pulses with durations of 7 and 20 ns were used in [15], and a high value of 16 γ_2 = (3.9±0.5)·10⁻¹⁶ and γ_2 = $(4.9\pm0.6)\cdot10^{-16}$ cm² W⁻¹ at 1064 nm were respectively obtained. This great dependence upon the pulse duration has been explained by the influence of electrostriction. As discussed above, this is not true in our opinion. Hence, the other reasons for explaining this significant deviation of obtained γ_2 values from the known ones for fused silica should exist. We think that the use of MLM pulses is not the best choice for the Z-scan experiments because the procedure of measuring and processing the data is very tedious and cannot ensure the true results.

Hence, we present here the results obtained using the MLM pulses for illustrative purposes only. We did not use the whole required procedure described above for processing the data obtained with MLM pulses. We have assumed that in our case most of generated pulses have the time profiles close to those shown in Fig. 2(c). Therefore, it has been assumed that the averaged values are practically the same as for this typical pulse. Using a previously described technique we calculated the coefficient $\eta^{(1)}_{\rm MLM} \approx$ 1.9. Then the described processing procedure was applied to the data obtained with MLM pulses of the Nd:YAG minilaser with the pulse energy $W_{\rm L} = 0.68$ mJ (Fig. 4(c)). The obtained results are presented in Table 3. First of all, it is seen from Fig. 4(c) that error bars are much larger than in Fig. 4(b). Secondly, from Fig. 4(c) we can see that the registered phase change $\langle \Delta \Psi_{0j}(t) \rangle_{\text{fit}}$ is notably higher (1.4 times). It means that the on-axis intensity and the transmittance induced by MLM laser pulses are also higher, although lower pulse energies have been used. It is seen from Tables 1–3 that a very good compatibility between the values of γ_2 is obtained using different pulses. Thus, practically the same values of nonlinear coefficient γ_2 for the samples of fused silica are obtained when using the Z-scan technique only if the temporal shapes of the used pulses are properly taken into account.

4. Conclusion

It is shown that the nonlinear refractive index coefficient n_2 of fused silica (one of the smallest among the condensed media) can be successfully measured by the Z-scan techniques using the pulses of simple and

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	$M^2 = 1.33$	$M^{2} = 1$	All parameters fitted
z_0	75.67±0.19 mm	74.54±0.38 mm	74.67±0.19 mm
$z_{ m R}$	8.89 mm (fixed)	11.83 mm (fixed)	8.91±0.29 mm
a	$(5.53 \pm 2.64) \cdot 10^{-6}$	$(1.92 \pm 3.43) \cdot 10^{-6}$	$(5.61 \pm 3.00) \cdot 10^{-6}$
ΔT	$(0.00 \pm 1.11) \cdot 10^{-4}$	$(0.00 \pm 1.38) \cdot 10^{-4}$	$(0.00 \pm 1.12) \cdot 10^{-4}$
$\langle \Delta \Psi_0(t) \rangle_{\rm fit}$	$(5.81 \pm 0.14) \cdot 10^{-2}$	$(5.16 \pm 0.15) \cdot 10^{-2}$	$(5.80 \pm 0.15) \cdot 10^{-2}$
γ_2	$2.59 \cdot 10^{-16} \text{ cm}^2 \text{ W}^{-1}$	$2.30 \cdot 10^{-16} \text{ cm}^2 \text{ W}^{-1}$	$2.58 \cdot 10^{-16} \text{ cm}^2 \text{ W}^{-1}$
n_2	$0.90 \cdot 10^{-13}$ esu	$0.80 \cdot 10^{-13}$ esu	$0.89 \cdot 10^{-13}$ esu

Table 3. Values of appropriate parameters obtained by different fitting procedures in the case when MLM pulses were used.

robust actively or passively Q-switched diode pumped Nd:YAG minilasers with durations of about 1 ns and energies less than 1 mJ. Good compatibility between the values of n_2 or γ_2 for the same samples of fused silica is obtained only if the temporal shapes of the used SBScompressed, SLM or MLM pulses are properly taken into account. It is also shown that spatial properties of the used beams should be taken into account properly. The obtained results confirm our opinion that the contribution of electrostriction to the value of n_2 is small enough (less than 15%) for stationary conditions and is practically negligible for used pulses shorter than 1 ns.

References

- R.L. Sutherland, with contributions by D.G. McLean and S. Kirkpatrick, *Handbook of Nonlinear Optics*, Optical Engineering Vol. 82, 2nd ed. (Marcel Dekker, Inc., New York, 2003).
- [2] Self-focusing: Past and Present. Fundamentals and Prospects, Topics in Applied Physics Vol. 114, eds.
 R.W. Boyd, S.G. Lukishova, and Y.R. Shen (Springer, 2009).
- [3] D.N. Christodoulides, I.C. Khoo, G.J. Salamo, G.I. Stegeman, and E.W. Van Stryland, Nonlinear refraction and absorption: mechanisms and magnitudes, Adv. Opt. Photon. 2(1), 60–200 (2010).
- [4] M. Rumi and J.W. Perry, Two-photon absorption: an overview of measurements and principles, Adv. Opt. Photon. 2(3), 451–518 (2010).
- [5] M. Sheik-Bahae, A.A. Said, T.-H. Wei, D.J. Hagan, and E.W. Van Stryland, Sensitive measurement of optical nonlinearities using a single beam, IEEE J. Quantum Electron. 26(4), 760–769 (1990).
- [6] "Discovering" Z-scan; Celebrating the Z-scan Technique, IEEE LEOS Newsletter **21**(1), 28–29 (2007).
- [7] P.B. Chapple, J. Staromlynska, J.A. Hermann, and T.J. Mckay, Single-beam Z-scan: measurement techniques and analysis, J. Nonlinear Opt. Phys. Mater. 6(3), 251–293 (1997).
- [8] E.W. Van Stryland and M. Sheik-Bahae, Z-scan measurements of optical nonlinearities, in: *Characteri*-

zation Techniques and Tabulations for Organic Nonlinear Materials, Optical Engineering Vol. 60, eds. M.G. Kuzyk and C.W. Dirk (Marcel Dekker Inc., New York, 1998) pp. 655–692.

- [9] G.L. Wood and E.J. Sharp, Nonlinear Optics, in: *Electro-Optics Handbook*, 2nd ed., eds. R.W. Waynant and M.N. Ediger (McGraw-Hill, New York, 2000) pp. 13.1–13.28.
- [10] M. Sheik-Bahae and M.P. Hasselbeck, Third-order optical nonlinearities, in: *Handbook of Optics*, Vol. IV, 3rd ed., ed. M. Bass (McGraw-Hill, New York, 2009) pp. 16.1–16.36.
- [11] A. Dement'ev, A. Jovaiša, and R. Navakas, Modified Z-scan method for determination of nonlinear refraction of optical materials through the measurement of power-weighted timeaveraged beam propagation factor, Proc. SPIE 4932, 286–295 (2003).
- [12] B. Gu, X-Q. Huang, S.-Q. Tan, and H.-T. Wang, A precise data processing method for extracting $\chi^{(3)}$ from Z-scan technique, Opt Commun. **277**, 209–213 (2007).
- [13] L. Pálfalvi, B.C. Tóth, G. Almási, J.A. Fülöp, and J. Hebling, A general Z-scan theory, Appl. Phys. B 97, 679–685 (2009).
- [14] T. Shimada, N.A. Kurnit, and M. Sheik-Bahae, Measurement of nonlinear index by a relay-imaged top-hat Z-scan technique, Proc. SPIE 2714, 52–60 (1996).
- [15] T. Olivier, F. Billard, and H. Akhouayri, Nanosecond Z-scan measurements of the nonlinear refractive index of fused silica, Opt. Express 12(7), 1377–1382 (2004).
- [16] A. Dement'ev and A. Jovaisa, Pulse shape influence on the accuracy of Z-scan measurements, Nonlin. Analysis Model. Control 10(2), 119–136 (2005).
- [17] R. Adair, L.L. Chase, and S.A. Payne, Nonlinear refractive index of optical crystals, Phys. Rev. B 39(5), 3337–3350 (1989).
- [18] A.J. Taylor, G. Rodriguez, and T.S. Clement, Determination of n_2 by direct measurement of the optical phase, Opt. Lett. **21**(22), 1812–1814 (1996).
- [19] D. Milam, Review and assessment of measured values of the nonlinear refractive-index coefficient of fused silica, Appl. Opt. 37(3), 546–550 (1998).
- [20] J.E. Aber, M.C. Newstein, and B.A. Garetz, Femtosecond optical Kerr effect measurements in silicate glasses, J. Opt. Soc. Am. B 17(1), 120–127 (2000).

- [21] Y.-F. Chen, K. Beckwitt, F.W. Wise, B.G. Aitken, J.S. Sanghera, and I.D. Aggarwal, Measurement of fifth- and seventh-order nonlinearities of glasses, J. Opt. Soc. Am. B 23(2), 347–352 (2006).
- [22] A.V. Smith and B.T. Do, Bulk and surface laser damage of silica by picosecond and nanosecond pulses at 1064 nm, Appl. Opt. **47**(26), 4812–4832 (2008).
- [23] A. Dement'ev, R. Buzelis, E. Kosenko, E. Murauskas, and R. Navakas, Solid-state lasers with pulse compression by transient stimulated Brillouin and Raman scattering, Proc. SPIE 4415, 92–97 (2001).
- [24] S.A. Akhmanov, R.V. Khokhlov, and A.P. Sukhorukov, Self-focusing, self-defocusing and self- modulation of laser beams, in: *Laser Handbook*, Vol. 2, ed. F.T. Arecchi (North-Holland, 1972), pp. 1151–1228.
- [25] V.N. Lugovoy and A.M. Prokhorov, Teoriya rasprostraneniya moshchnogo lazernogo izlucheniya v nelineynoy srede, Usp. Fiz. Nauk 111(2), 203–247 (1973) [in Russian; English translation: Sov. Phys. Usp. 16(5), 658 (1974)].
- [26] O. Svelto, Self-focusing, self-trapping, and self-phase modulation of laser beams, in: *Progress in Optics*, Vol. XII, ed. E. Wolf (North-Holland, 1974) pp. 1–31.
- [27] R.W. Hellwarth, Third-order optical susceptibilities of liquids and solids, Prog. Quantum Electron. 5, 1–68, (1977).

- [28] R.W. Boyd, *Nonlinear Optics*, 3rd ed. (Academic Press, 2008).
- [29] A.S. Dement'ev, E.K. Maldutis, and S.V. Sakalauskas, Optical anisotropy, induced in glasses by intensive laser radiation, Quantum Electronics (Kiev) 15, 62–76 (1978) [in Russian].
- [30] A.S. Dement'ev, E.K. Maldutis, and S.V. Sakalauskas, Electrostrictive change of refraction index of glasses in elliptical laser beams, Opt. Spektrosk. [Opt. Spectrosc., in Russian] 50(1), 143149 (1981).
- [31] A. Dementjev, D. Steponavičius, and R. Buzelis, Quality parameters of general astigmatic laser beams and their measurement, Matavimai Nr. 1(25), 7–13 (2003) [in Lithuanian].
- [32] A. Dementjev, R. Navakas, R. Čiegis, and G. Šilko, Analysis of the ISO alternative measurement methods of laser beam widths and propagation factors, Matavimai Nr. 4(28), 17–22 (2003) [in Lithuanian].
- [33] A.S. Dementjev, A. Jovaisa, G. Silko, and R. Ciegis, On alternative methods for measuring the radius and propagation ratio of axially symmetric laser beams, Quant. Electron. 35(11), 1045–1052 (2005).
- [34] N.Y. Tabiryan, V. Jonnalagadda, M.J. Mora, and S.R. Nersisyan, Laser beam and optics characterization with "z-scan" method, Proc. SPIE 4932, 656–666 (2003).

Z SKENAVIMO MATAVIMŲ PRIKLAUSOMYBĖ NUO ERDVINIŲ IR LAIKINIŲ IMPULSŲ PARAMETRŲ

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Santrauka

Pateikiami Z skenavimo su uždara apertūra eksperimentiniai rezultatai, kuriems gauti naudoti Nd: YAG minilazerio trumpi impulsai su skirtingomis laikinėmis impulsų formomis. Parodyta, kad netiesinio lūžio rodiklis n_2 kvarciniam stiklui (vienas iš mažiausių kondensuotoms terpėms) gali buti sėkmingai išmatuotas naudojant impulsus, kurių trukmė apie 1 ns ir energija mažesnė negu 1 mJ. Labai geras išmatuotų verčių suderinamumas gaunamas tik tada, kai apdorojant rezultatus yra deramai atsižvelgiama į priverstinės Brijueno sklaidos kompresijos metu gaunamas ir vienos bei kelių išilginių modų generuojamų impulsų formas. Taip pat parodyta, kad apdorojant rezultatus reikia teisingai įskaityti naudojamų pluoštų erdvinius parametrus. Šiais eksperimentais akcentuojama impulsų formos įskaitymo svarba vertinant medžiagų netiesinį lūžio rodiklį iš Z skenavimo eksperimentinių duomenų.