ANALYSIS OF PARAMETRIC FLUORESCENCE AMPLIFIED IN A NONCOLLINEAR OPTICAL PARAMETRIC AMPLIFIER PUMPED BY THE SECOND HARMONIC OF A FEMTOSECOND Yb:KGW LASER

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We present the results of theoretical and experimental investigation of amplified parametric fluorescence (APF) produced in a high-gain BBO-based femtosecond noncollinear optical parametric amplifier (OPA) pumped at 515 nm. Differences of APF levels in Poynting vector walk-off-compensating and tangential phase-matching amplification geometries are examined. APF suppression due to the presence of a seed pulse in the OPA is measured and is found to be around 6 times in typical OPA operating conditions when pump-to-signal conversion efficiency is 11.5%.

Keywords: parametric fluorescence, optical parametric amplifier, contrast

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1. Introduction

Optical parametric chirped-pulse amplification (OPCPA) [1] is a well-established method to produce high-energy, few-cycle pulses. This technique allows one to reach a gain of more than $10^6$ in a single pass of a few millimetre long crystal. However, this gain is attainable only by using high pump intensities in the amplifier crystal, which in turn increases the probability of efficient parasitic generation and amplification of optical parametric fluorescence. Consequently, amplified parametric fluorescence (APF) degrades signal stability and reduces extractable signal energy due to transfer of pump energy to the incoherent pedestal [2]. This lowers the compressed pulse contrast (ratio of the intensities of the amplified pulse and incoherent background), which is a major concern in high-field experiments. APF is only produced within the temporal window defined by the pump pulse, therefore it is proposed that using a short pump pulse in the first amplification stage, in which typically high gain is required, can increase pulse contrast at the OPCPA output [3]. The short-pulse preamplification approach was demonstrated in an OPCPA system driven by femtosecond ytterbium and picosecond neodymium pump sources [4].

APF is a result of parametric amplification of quantum noise due to two-photon emission from a virtual level excited by the intense pump field and stimulated by the signal and idler field zero-point fluctuations [5, 6]. For a long time APF was successfully used as a seed source for tunable optical parametric amplifiers (OPAs) pumped by picosecond pulses [7, 8]. However, the output of OPAs of this type exhibits high shot-to-shot pulse energy fluctuations, typically far exceeding those of the pump laser, possibly with individual shots entirely missing from the pulse train. From these high fluctuations one might infer that in the case of tight pump focusing, APF originates from a relatively low number of quantum noise photons, which, however, can be amplified to significant energies due to the high gain in parametric amplification systems. So far, works discussing the origin and amount of APF in OPA and OPCPA systems have not been numerous [9–14]. Efficient broad-band parametric amplification in the BBO crystal can be achieved by directing the signal beam at the so-called magic angle to the pump beam, which is about 2.5° (inside the crystal) in the case of 515 nm pump. However, due to crystal birefringence the direction of the pump Poynting vector differs from that of the pump wave vector and the degree of spatial overlap between pump, signal, and idler beams depends on the orientation of the nonlinear crystal. In one orientation, the Poynting vector walk-off leads to better spatial overlap of pump and signal beams (see Fig. 1(a)); this

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geometry is called Poynting vector walk-off compensation geometry (PVWC) \[15\]. In the case of the other orientation of the optical axis (see Fig. 1(b)) – tangential phase-matching geometry (TPM) – the pump beam propagates very close to that of the angular dispersed idler beam. Both geometries are commonly used in noncollinear optical parametric amplifiers and allow for similar pump-to-signal conversion efficiencies. However, the spatial and spectral parameters of the amplified signal differ appreciably due to specific spatio-temporal pulse shaping dynamics and different parasitic frequency mixing processes in PVWC and TPM geometries. The PVWC geometry offers a much better near-field profile of the signal beam, however, the signal is accompanied by the parasitic second harmonic generation affecting the shape of the amplified spectrum \[16\]. On the other hand, numerical simulations have confirmed that undesirable spectral phase modulation of the signal pulse occurs in the TPM geometry \[17\]. Differences are more pronounced when narrow beams and short pulses are used in parametric amplifiers. As the contrast of an OPCPA system output is usually defined by the first amplification stage \[13\], the common practice is to design these first stages to operate with minimum beam sizes in order to enhance the ratio of seed and quantum noise photons in the amplification channel. Different spatio-temporal parametric amplification conditions in PVWC and TPM amplification configurations may also lead to different APF levels at the output of OPA. However, to the best of our knowledge, this issue has not yet been examined.

In this work we investigate the properties of APF produced in a high-gain BBO-based femtosecond noncollinear optical parametric amplifier (NOPA) pumped at 515 nm and examine the differences of APF levels in two different amplification geometries.

2. Theoretical modelling

2.1. Governing equations

The computer simulations of noncollinear parametric amplification were performed using nonlinear coupling equations that in the Fourier domain can be expressed as

$$\frac{\partial^2}{\partial z^2} S_j + (k^2(\omega_j) - k_s^2 - k_i^2) S_j = -\mu_0 \omega_j^2 \hat{P}_j,$$

where \(j = 1, 2, 3\) stands for signal, idler and pump waves, respectively. \(S_j(\omega_j, k_s, k_i)\) are the Fourier transforms of electric fields \(A(t, x, y)\). \(k\) is a wave number and \(k_s, k_i\) are the projections of the wave vector. We consider the Cartesian coordinates \((x, y, z)\). Time and cyclic frequency are denoted by \(t\) and \(\omega\), respectively. \(\mu_0\) is the vacuum permeability and \(\hat{P}_j\) is the Fourier transform of a nonlinear polarization.

We investigated the nonlinear Type I interaction in the BBO crystal. The signal and idler waves are ordinary and their wave numbers depend only on cyclic frequency \(\omega\). The wave number of the pump wave is...
depends also on the propagation direction (projections \( k_x \) and \( k_y \)).

From Eq. (1) it follows that
\[
\begin{align*}
\frac{\partial}{\partial z} S_1 &= i k_{x1} S_1 - \frac{\mu_0 \omega_1^2}{2 i k_{z1}} \hat{P}_1, \\
\frac{\partial}{\partial z} S_2 &= i k_{x2} S_2 - \frac{\mu_0 \omega_2^2}{2 i k_{z2}} \hat{P}_2, \\
\frac{\partial}{\partial z} S_3 &= i k_{x3} S_3 - \frac{\mu_0 \omega_3^2}{2 i k_{z3}} \hat{P}_3,
\end{align*}
\]
(2)

where \( k_{x1,2} = \sqrt{k(\omega_{x,2})^2 - k_x^2 - k_y^2} \) and \( k_{x3} = \sqrt{k(\omega_{x,3}, k_x, k_y)^2 - k_x^2 - k_y^2} \).

Equation (2) was solved by a Fourier split-step method. The linear part was solved in the Fourier domain:
\[
S_j(z + h_z) = S_j(z) \exp(i k_{x1} h_z - i h_z(\omega - \omega_0)/u_j),
\]
(3)

where \( h_z \) is the longitudinal step. The second term in the brackets was subtracted in order to reduce the time walk-off. We set \( u_j = c/1.65 \), where \( c \) is the speed of light. The nonlinear part was solved for the fields \( A_j \) which were found by the use of the inverse Fourier transform of \( S_j \). The simplifications were performed applying the paraxial approximation for the wave packets: the factors \( \mu_0 \omega_j^2/(2 i k_{zj}) \) in the nonlinear terms were substituted by their values at \( \omega_j = \omega_{j0}, k_x = k_y = 0 \), where \( \omega_{j0} \) is the central frequency of the \( j \)th wave. \( k_z = k_y = 0, k_{zj} = k_{zj0} \).

To order to describe quantum noise fluctuations we added the Langevin noise terms \( \eta_j \). First, we note that \( A_j = B_j \exp(i k_{xj} z) \). The nonlinear and noise part of the equations was solved for amplitudes \( B_j \) as follows:
\[
\begin{align*}
B_1(z + h_z) &= B_1(z) + h_z \left[ -\Gamma B_1(z) + \sigma_1 B_1^2(z) B_3(z) \exp(i \Delta k z) + \xi_1 \sqrt{2 \Gamma/h_z} \right], \\
B_2(z + h_z) &= B_2(z) + h_z \left[ -\Gamma B_2(z) + \sigma_2 B_1^2(z) B_3(z) \exp(i \Delta k z) + \xi_2 \sqrt{2 \Gamma/h_z} \right], \\
B_3(z + h_z) &= B_3(z) + h_z \left[ -\Gamma B_3(z) - \sigma_3 B_1^2(z) B_2(z) \exp(-i \Delta k z) + \xi_3 \sqrt{2 \Gamma/h_z} \right] \\
& - \xi_1 B_1(z) B_3(z) \exp(-i \Delta k z) + \xi_2 B_2(z) \exp(i \Delta k z),
\end{align*}
\]
(4)

Here \( \Delta k = k_{z30} - k_{z20} - k_{z10} \) is the phase mismatch. We note that the Langevin noise term \( \xi_j \) is \( \delta \)-correlated:
\[
\langle \eta(t, x, y, z) \eta(t', x', y', z') \rangle = \eta_0 \delta(x-x') \delta(y-y') \delta(t-t') \delta(z-z').
\]
(5)

Here \( \tau \) and \( \rho \) are the pulse duration and beam radius, respectively. \( k_{z10} \) is the \( x \) projection of the input signal beam wavevector. The sign '+' before it corresponds to PVWC amplification configuration, i.e. the pump walk-off towards the seed beam direction (see Fig. 1(a)). Sign '-' corresponds to TPM geometry (see Fig. 1(b)). \( a_{10} \) and \( a_{30} \) are the amplitudes of signal and pump pulsed beams, respectively. \( \gamma \) is the chirp parameter. \( \xi_{1,20} = \xi_{1,20}(x, y, t) \) is the input noise. Computer simulations were performed using the wavelength, beam size, pulse duration and pulse energy values corresponding to those used in the experiment. However, Gaussian pulse and beam shapes were assumed and no attempt was made to replicate the experimental conditions exactly. As we can see from Eq. (7), the input signal wave is a chirped pulse. The pump wavelength was set to \( \lambda_{30} = 515 \) nm. We assume the noncollinearity angle for the signal beam to be \( \alpha_{10} = 2.56^\circ \) which was calculated by the use of Selmeier equations from [18]. The phase matching angle is \( \theta_3 = 24.5^\circ \) and the central signal wavelength is \( \lambda_{10} = 795 \) nm. The signal pulse chirp parameter is \( \gamma = 7.5 \). \( \rho_1 \) and \( \rho_2 \) are 250 and 110 \( \mu \)m at FWHM, respectively. The pulse duration \( \tau \) corresponds to 200 fs at FWHM. The crystal length is 2.5 mm and the input seed energy is 1 nJ. We also involved into consideration the nonlinear interaction length \( L_{nj} = 1/(\alpha_{30} \sigma) \). For the 2 \( \mu \)J pump energy (85 GW/\( \text{cm}^2 \) intensity) we obtain \( L_{n3} = 130 \) \( \mu \)m. \( d^{\text{eff}} \) was taken from [19].

For evaluation of the input noise intensity we use the formula from Ref. [11].
where $\hbar$ is the Plank constant and $n$ is the refractive index. $\Delta \omega$ is the detected spectral width and $\Delta \Omega$ is the solid angle of the emitted radiation. In the formula we have omitted an additional factor of 2 since we calculate signal and idler noises separately. For the wavelength window from 650 nm to 950 nm and the solid angle calculated from the divergence angle of the pump we obtain $I_{noise} = 2180$ W/m$^2$ that for the pulse duration of 200 fs corresponds to only 20 photons. We have to magnify the obtained values by $N^2$ since we consider the angular spectrum of the input signal noise with the divergence angle 2.5° which is $N\theta$ times larger than the divergence angle of the pump beam.

2.2. Results of numerical simulations

First, we have performed the modelling of parametric fluorescence amplification, i.e. the case when no seed is present at the OPA input. The angular spectrum of the APF signal beam is presented in Fig. 2. It was integrated over all frequency components. As we can see, the left side of the APF ring is brighter than the right one, though the pump walk-off for this case is on the opposite side with reference to the cone axis, i.e. corresponds to the situation depicted in Fig. 1(b). This non-intuitive result can be explained by the fact that in this case the propagation direction of the idler beam nearly coincides with the pump beam. The propagation angle of the idler is larger than that of the signal, so it can better follow the pump beam during its walk-off.

In order to evaluate the amplified signal energy contrast with reference to APF we have repeated calculations of angular output radiation distribution in the presence of seed. The seed is directed into the crystal at the internal non-collinearity angle $\alpha_{10} = 2.56^\circ = 45$ mrad. PVWC and TPM configurations were examined simply by taking positive or negative $\alpha_{10}$ values, i.e. choosing $+k_{x10}$ or $-k_{x10}$ in Eq. (7). The light energy variation on the cone obtained by scanning it with a rectangular spatial aperture with a size of 18 mrad is depicted in Fig. 3. The red curve (1) which shows the APF angular distribution when seed is absent (see Fig. 2) indicates that APF intensity on the right and left sides of the cone (see the points at 0 and 180 deg angles) differs by about one order of magnitude (more than 10 times).

![Fig. 3. Angular intensity distribution on the cone. Red (online) line 1 is APF energy when seed is blocked. Signal amplification in PVWC and TPM configurations is presented by blue (online) 2 and magenta (online) 3 lines, respectively. Pump intensity 170 GW/cm$^2$.](image)

When the seed is amplified in TPM geometry (the point on the magenta line at 180 deg), the amplified signal magnitude is higher than the APF level of an unseeded OPA (the point on the red line at 180 deg) by more than three orders of magnitude. The contrast ratio in the case of amplification in PVWC geometry is definitely higher, as the amplified pulse energy is smaller by ~1.2 times but the APF level is lower by an order of magnitude (see points at 0 deg on the blue and red line, respectively) as compared to the case of amplification in the TPM configuration. We point out that introducing the seed results in lowering of light intensity on the cone both for PVWC and TPM geometries. This

![Fig. 2. Angular spectrum of APF. Pump intensity 170 GW/cm$^2$.](image)
APF gain suppression is caused by pump depletion due to energy transfer to the signal and leads to overall APF levels lower by several times when the OPA is seeded, as compared to APF levels in an unseeded OPA.

The data on signal and APF amplification in PVWC and TPM geometries at various pump intensities are presented in Fig. 4. One can see that the PVWC configuration provides a notably higher ratio of the amplified signal energy with respect to the energy of APF in the amplification channel.

3. Experiment

In our setup a Yb:KGW diode-pumped solid state laser system (PHAROS, Light Conversion, Ltd.) generating 200 fs pulses at 1030 nm at a repetition rate of 1 kHz was used. A small part of the pulse energy (∼1 μJ) was split off and focused into a 4 mm sapphire plate to generate a white-light continuum (WLC) seed. A waveplate-polarizer attenuator was used to finely tune the pump energy for optimum WLC generation, which led to the WLC spectrum being highly stable on both shot-to-shot and day-to-day timescales. The larger part of the pulse energy was frequency doubled in a 0.7 mm BBO crystal, producing pump pulses for the NOPA. Parametric amplification was carried out in a 2.5 mm type-I BBO crystal into which the pump beam was focused to a spot size of 110 μm at FWHM. The size of the seed beam was 250 μm at FWHM. The phase matching angle of the crystal and the noncollinearity angle were fine-tuned for efficient signal amplification in the 670–950 nm spectral range. In our setup the continuum seed pulse with an energy content of ∼5 nJ in the 670–950 nm spectral band could be amplified up to 0.6 μJ at a pump intensity level of 170 GW/cm² with a conversion efficiency of 11.5%. Parasitic SHG at a wavelength of 435 nm was observed in the case of PVWC configuration. This results in a hole in the amplified spectrum at ~870 nm.

When the seed is blocked, the cone of APF is clearly observed at high pump intensity levels. The half-angle of the cone centered on the pump beam is set to ~4.1° (=71 mrad) by tuning the phase matching angle of the crystal. Since the refraction index of the BBO crystal is ~1.66 at 800 nm, this corresponds to an internal signal-pump noncollinearity angle of ~2.5° that is called the magic angle and provides the broadest spectral amplification band. An image of APF spatial distribution acquired with a beam profiling camera (WinCamD, DataRay Inc) is presented in Fig. 5(a). To avoid saturation of the detector, the pump beam had to be blocked with an appropriate dielectric mirror. Additionally, several calibrated neutral density filters were
used for measuring the superfluorescence at different levels of pumping. The difference between the APF amplitudes on the right and left sides of the cone arises due to varying the pump beam spatial overlap with an amplified signal or idler waves of parametric fluorescence. In this case the orientation of the optical axis corresponds to that which is shown in Fig. 1(b).

We have measured the dependence of APF on pump intensity at different angles on the cone (1, 2, 3 marked in Fig. 5(a)). The results presented in Fig. 5(b) show, as expected, the exponential APF intensity dependence on pump intensity for all three measured directions on the cone.

The amount of APF in the amplification channel measured by blocking the seed is the worst case assessment of the amplified pulse energy contrast. The presence of the seed at the input of OPA suppresses APF since even a small depletion of the pump pulse due to energy transfer to the injected signal reduces the amplification of parametric fluorescence [13]. To the best of our knowledge, the amount of APF suppression has so far only been measured in a single work [14] by creating a narrow spectral hole in the seed spectrum using an acousto-optic pulse shaper. In contrast, we have examined the APF suppression by measuring the APF intensity at the point on the APF cone that was away from the signal amplification channel, i.e. the 2nd zone in Fig. 1(a). The light was collected by a 400 μm diameter fiber and measured using a compact spectrometer (AvaSpec 3648, Avantes). Spectra acquired with the seed blocked and unblocked at different pump intensity levels were integrated in the wavelength region of our interest (670–950 nm). The obtained results are presented in Fig. 6(a). APF suppression up to 6 times was measured when pump-to-signal energy conversion reached 11.5% at a pump intensity of 170 GW/cm² (see Fig. 6(b)). These results are close to the APF suppression ratio obtained by computer simulations (see Fig. 3).

The results of theoretical treatment presented in Section 2 show that the level of APF in PVWC and TPM non-collinear parametric amplification geometries differs considerably. In order to verify this finding experimentally we have measured the energies of both the amplified signal and APF (by blocking the seed) for the both amplification geometries. In our experimental conditions the APF at low pump intensities is very weak and cannot be measured directly by our standard power meter. In order to evaluate APF energies we blocked the seed and measured the spectra of APF propagating in the signal amplification channel. The energies of APF were calculated by taking spectra integrals over a range of 670–950 nm and scaling it by a factor, which was found by comparing energy values measured with a spectrometer and a power meter at high pump intensity levels above 160 GW/cm².

The obtained data are presented in Fig. 7 and show that one obtains a bit higher amplified signal energy in the TPM geometry. However, the APF energy level for different interaction geometries differs significantly and the APF energy content at the OPA output is less than 0.1% even in the strong amplification saturation regime in the PVWC configuration. When accounting for the APF suppression effect one can expect several times lower values of parametric fluorescence. The dashed lines in Fig. 7 show the expected levels of APF calculated by applying the suppression factor derived from the data presented in Fig. 6(a). The amplified pulse contrast steadily drops with increasing pump intensity: seed amplification saturates, while the steadily rising contribution of APF from the temporal areas where the level of seed is low leads to a monotonous increase of an incoherent
background. Therefore, looking for the best trade-off between the high output energy and the low APF level, we consider the pump level of 140–170 GW/cm² to be optimum. We also note that for pump levels above 180 GW/cm² we observed undesirable modulations in the amplified pulse spectrum and the spatial profile caused by nonlinear self-action processes in the BBO crystal. The results of numerical modelling (see Section 2) show higher absolute values of the ratio of the amplified signal and APF as compared to the same ratios measured in the experiment. This can be explained by the fact that the computer simulations were performed for ideal wave packets with both spatial and temporal Gaussian profiles, while the characteristics of real pulses in the experiment were different to some extent. Nevertheless, the numerical and experimental results agree well qualitatively. It is seen that in the case of noncollinear parametric amplification of low intensity seed pulses the PVWC geometry has a considerable advantage over the TPM configuration in terms of a notably higher amplified pulse contrast.

4. Conclusions

We have investigated the properties of APF produced in a femtosecond NOPA that will serve as a front end in a TW-class OPCPA system [20] and examined the two possible geometric configurations of broadband noncollinear parametric amplification in the BBO crystal pumped by 515 nm pulses. The presented experimental and numerical results reveal that PVWC amplification geometry provides APF levels that are lower by an order of magnitude as compared to amplification in TPM geometry. Furthermore, we have used an original method to determine the level of APF suppression due to pump depletion by the signal and found it to be slightly smaller than 1 order of magnitude in typical OPA operating conditions. We believe that these findings are relevant for the optimization of OPCPA system designs for higher output pulse contrast.

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References


NEKOLINEARIAUS OPTINIO PARAMETRINIO STIPRINTUVO KAUPINAMO ANTRA FEMTOSEKUNDINIO Yb:KGW LAZERIO HARMONIKA PARAMETRINĖS FLUORESCENSIJOS TYRIMAS

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Santrauka

Pristatomas tyrimas, skirtas surasti optimalias nekolinearus optinio parametrinio stiprinimo sąlygas BBO kri stalė kaupinant femtosekundine 515 nm bangos ilgio spinduliuote, pagrindinį dėmesį skiri ant toms sąlygoms, kurios leistų pasiekti geresnį stiprinimo signalinio impulsu kontrastą. Pasitelkus teorinių modeliavimą ir eksperimento rezultatus nustatyta, kad nepageidaujamos sustiprintos parametrinės fluorescencijos (SPF) lygis gerokai skiriasi įspūdingai į pasirinktą vieną iš dviejų galimų stiprinimo geometrijų. Be to, naują metodą pa- lyginus SPF intensyvumą vykstant užkrato stiprinimui ir be jo, nustatyta, kad kaupinimo nuskurdinimo atveju SPF lygis sumažėja 6 ir daugiau kartų, kai keitimo iš kaupinimo į signalą efektyvumas pasieka 11,5 %.